

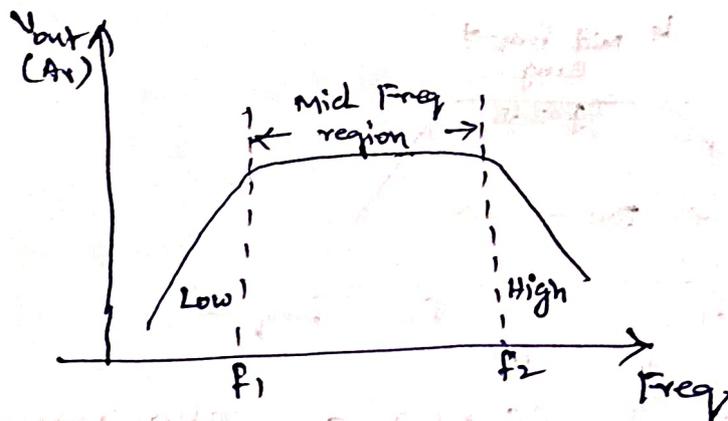
Unit-II

Frequency Response

Low Freq. Response of the CS and CE amplifiers, Internal Capacitive Effect and the High-Freq. Model of the MOSFET and the BST, High Freq. Response of the CS, follower, CE, CG and cascade Amplifier.

Introduction:-

* The frequency Response curve is a plot of the voltage gain of an amplifier against the freq. of I/p signal.



* I/p volt is kept constant & freq. of I/p signal is continuously varied.

* The o/p volt at each freq. of I/p signal is noted and the gain of the amplifier is calculated.

* The o/p volt. or gain is then plotted against frequency.

* Note: AF amplifier freq. range is 20 Hz to 20 kHz.

* The freq. response is ideal over a wide range of mid-freq.

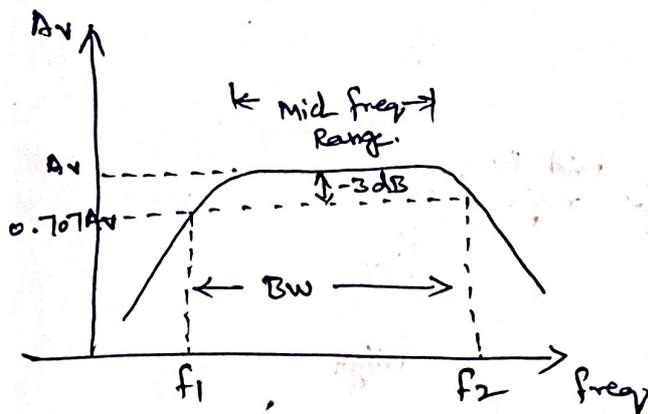
* At low & high freq. ends, the gain deviated from ideal characteristics.

* The decrease in voltage gain with freq. is called roll-off.

* Bandwidth of the amplifier is defined as the difference b/w f_2 and f_1 . (i.e., $BW = f_2 - f_1$)

where, f_2 - high freq. Region

f_1 - Low freq. Region.

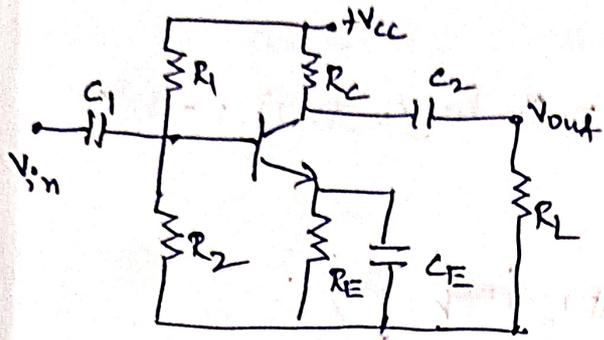


* These two freq. (f_1 & f_2) are also referred to as half-power freq. since gain or o/p volt. drop to 70.7% of maxi value and this represents a power level of ~~half~~ one-half the power at the reference freq. in mid-freq. region.

$$\text{Volt. gain in dB} = 20 \log A_v$$

$$\text{Power gain in dB} = 10 \log A_p$$

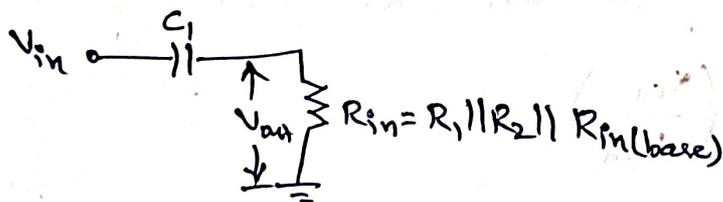
Low Freq Response of CE Amplifier:-



* RC N/w that affect its gain as the freq is reduced below midrange. These are,

- ① RC N/w formed by the C_1 and I/p impe. of amplifier.
- ② RC N/w formed by o/p C_2 and an collector resistance and R_L .
- ③ RC N/w formed by C_E and R_E .

* I/p RC N/w:



- As per po volt. divider theorem,

$$V_{out} = \left(\frac{R_{in}}{\sqrt{R_{in}^2 + X_{C1}^2}} \right) V_{in}$$

Where, X_{C1} - capacitance

- A critical point in the amplifier response is generally accepted to occur when the o/p volt is 70.7% of the I/p.

$$\text{i.e.; } \frac{R_{in}}{\sqrt{R_{in}^2 + X_{C1}^2}} = 0.707 = \frac{1}{\sqrt{2}}$$

At this condition, $R_{in} = X_{C1}$

* overall gain reduced due to the Attenuation provided by the I/P RC N/w.

$$A_v = 20 \log \left(\frac{V_{out}}{V_{in}} \right) = 20 \log(0.707) = -3 \text{ dB}$$

* Lower critical (cut-off) freq is,

$$f_c = \frac{1}{2\pi R_{in} C_1} = \frac{1}{2\pi (R_1 || R_2 || h_{ie}) C_1}$$

with source Resistance,

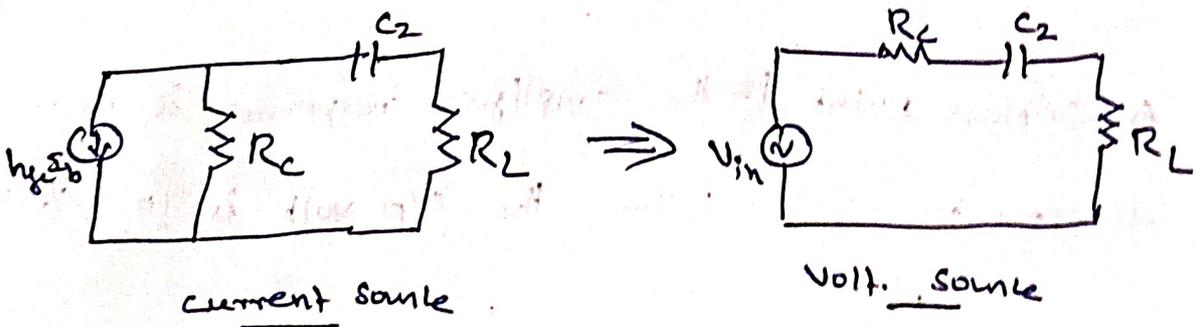
$$f_c = \frac{1}{2\pi (R_s + R_{in}) C_1}$$

* phase angle in an I/P RC ckt is,

$$\theta = \tan^{-1} \left(\frac{X_{C1}}{R_{in}} \right)$$

2. output RC Network:-

- o/p RC N/w formed by C_2 , resistance looking in at the collector and the load Resistance.

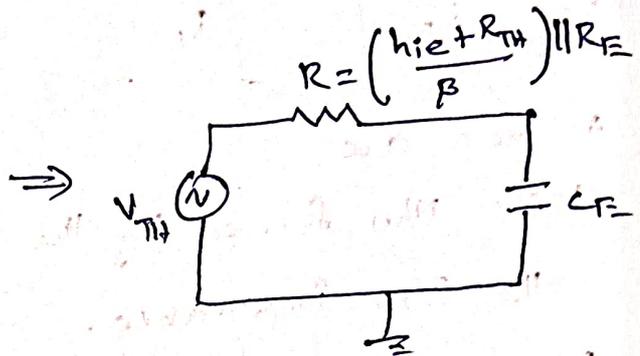
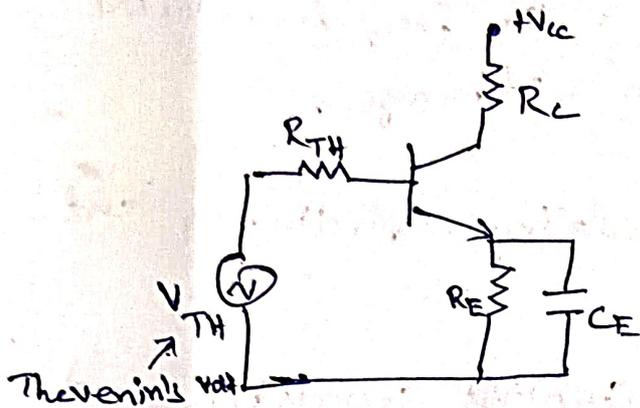


* critical freq, $f_c = \frac{1}{2\pi (R_c + R_L) C_2}$

* phase angle, $\theta = \tan^{-1} \left(\frac{X_{C2}}{R_c + R_L} \right)$

③ Bypass N/w

Sto RC N/w formed by the emitter bypass capacitor C_E and the resistance looking in at the emitter.



* Here, $\frac{h_{ie} + R_{TH}}{\beta}$ is the resistance looking in at the emitter.

It is derived as follows,

$$R = \frac{V_e}{I_e} + \frac{h_{ie}}{\beta} \approx \frac{V_b}{\beta I_b} + \frac{h_{ie}}{\beta} = \frac{I_b h_{ie}}{\beta I_b} + \frac{h_{ie}}{\beta} = \frac{R_{TH} + h_{ie}}{\beta}$$

[where, $V_e = V_b$
 $I_c = \beta I_b$; $I_e = I_c$]

* Critical freq,

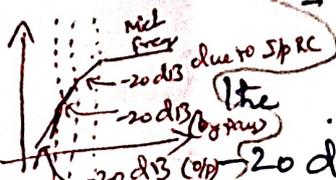
$$f_c = \frac{1}{2\pi R C_E} = \frac{1}{2\pi \left[\left(\frac{h_{ie} + R_{TH}}{\beta} \right) || R_E \right] C_E}$$

Notes:-

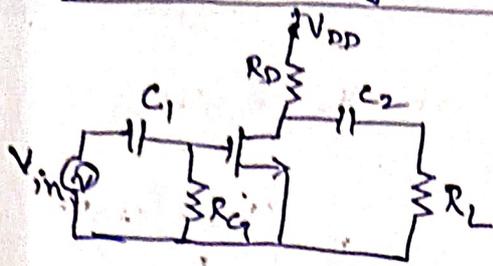
- Each N/w has a critical freq. It is not necessary that all these freq, should be equal.

- The N/w which has higher critical freq, than other two N/w is called dominant N/w.

The dominant N/w determines the freq, at which the overall gain of the amplifier begin to drop at 20 dB/decade.



Low Frequency Analysis of CS Amplifier:-



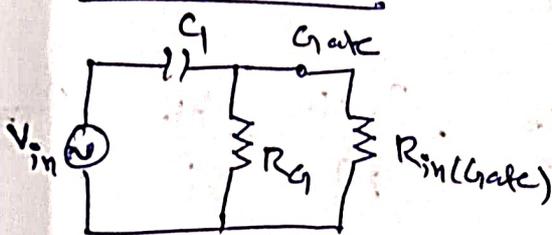
* Two RC N/w that affect the gain as the freq is reduced below midrange.

* There are,

① RC N/w formed by the I/P coupling capacitor C_1 and the I/P impedance.

② RC N/w formed by the O/P coupling capacitor and the output impedance looking in at the drain.

1. I/P RC N/w:-



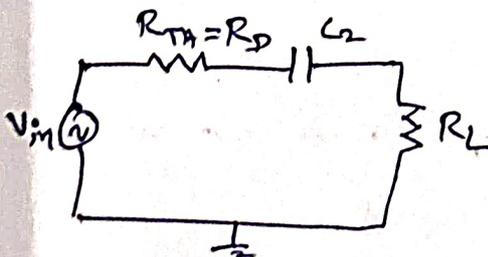
* RC N/w formed by C_1 and I/O impe of the amplifier.

* critical freq, $f_c = \frac{1}{2\pi R_{in} C_1}$

where $R_{in} = R_G \parallel R_{in}(gate)$

$R_{in}(gate) = \left| \frac{V_{ov1}}{I_{DSS}} \right|$ where, I_{DSS} is gate of

2. O/P RC N/w



* O/P RC N/w formed by C_2 and o/p impe. in at the drain

* critical freq, $f_c = \frac{1}{2\pi(R_D + R_L)C_2}$

* $\theta = \tan^{-1} \left(\frac{X_{C2}}{R_D + R_L} \right)$

Note: which N/w having high critical freq is called dominant N/w.

Internal Capacitances of MOSFET and High Freq. Model:-

* High freq. response of MOSFET affects due to internal capacitances.

* Two types of Internal Capacitances in the MOSFET:

① Gate capacitance: It is a parallel-plate capacitance formed by a gate electrode with the channel (C_{ox}) -oxide layer act as a capacitor dielectric

② Junction capacitance: (source-body, drain body depletion layer capacitances).

These capacitances are due to reverse biased pn junction by the n⁺ source region and p-type substrate and n⁺ drain region and p-type substrate.

① Gate capacitance:-

There are gate capacitance: C_{gs} , C_{gd} and C_{gg}

* Value of gate capacitances:

- In triode region, the channel has uniform depth

$$C_{gs} = C_{gd} = \frac{1}{2} WL C_{ox}$$

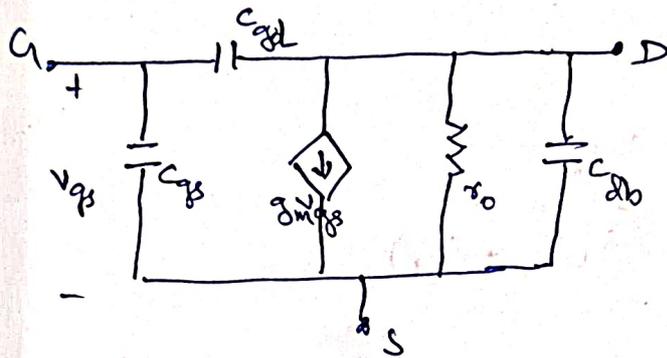
- In saturation region.

$$C_{gs} = \frac{2}{3} WL C_{ox}$$

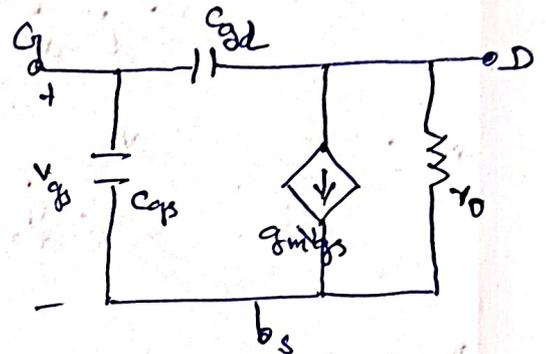
$$C_{gd} = 0$$

High-Frequency MOSFET Model:-

* Fig. shows the high freq, equ ckt model of MOSFET.
 In this model, capacitance C_{db} can be ~~negle~~ neglected to simplify the analysis.



(a) High Freq equ ckt Model.



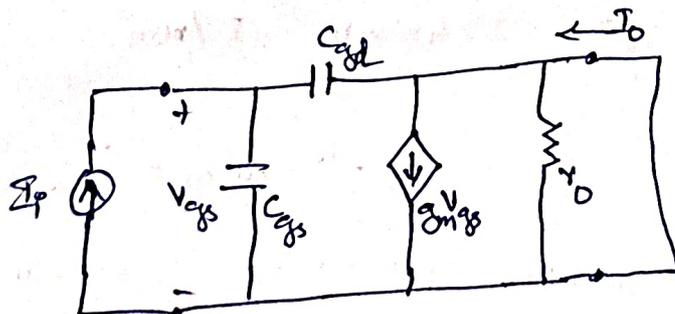
(b) High Freq equ. ckt neglecting C_{db}

Unity Gain Freq:- (f_T)

* The f_T is the freq, at which the ^{Short ckt} SC-ct gain of the CS MOSFET amplifier ~~gain~~ becomes unity.

* modified high-freq equ ckt to determine SC-ct gain.

- I/p is fed with a ct-source 'I_s' and o/p is SC.



High Freq model to determine SC-ct gain.

- In cut-off Region, the channel disappears, thus,

$$C_{gs} = C_{gd} = D \text{ (cut-off)}$$

However, gate-body model capacitance is,

$$C_{gb} = W L_{ov} C_{ox} \text{ (cut-off)}$$

- overlap capacitance (C_{gb} known as overlap capacitance).

$$C_{ov} = W L_{ov} C_{ox}$$

where, L_{ov} - overlap length (0.05L to 0.1L)

② Junction Capacitance:-

* Source diffusion capacitance is,

$$C_{sb} = \frac{C_{sbo}}{\sqrt{1 + \frac{V_{SB}}{V_0}}}$$

where, C_{sbo} - zero body-source bias,

V_{SB} - Reverse bias volt.

V_0 - Junction built in volt
(0.6 to 0.8V)

* Similarly, drain diffusion capacitance,

$$C_{db} = \frac{C_{dbo}}{\sqrt{1 + \frac{V_{DB}}{V_0}}}$$

* The sc-ct I_o is,

$$I_o = g_m V_{gs} - s C_{gd} V_{gs}$$

$$I_o = g_m V_{gs}$$

where, $s C_{gd} V_{gs}$ - small, so neglected.

* V_{gs} in terms of I_i is,

$$V_{gs} = \frac{I_i}{s(C_{gs} + C_{gd})}$$

$$\therefore \frac{I_o}{I_i} = \frac{g_m V_{gs}}{g_m s(C_{gs} + C_{gd})} = \frac{g_m}{s(C_{gs} + C_{gd})}$$

* $s = j\omega$, then mag. of ct becomes unity at the freq.

$$\omega_T = \frac{g_m}{C_{gs} + C_{gd}} \Rightarrow f_T = \frac{g_m}{2\pi(C_{gs} + C_{gd})}$$

$\therefore f_T$ proportional to g_m and Inversely proportional to Internl Capacitance

→ For n-channel MOSFET, $L = 1.0 \mu\text{m}$, $L_{gv} = 0.05$, $W = 10 \mu\text{m}$,
 $C_{ox} = 3.45 \times 10^{-3} \text{ F/m}^2$, $I_D = 200 \mu\text{A}$ and $k_n = 150 \mu\text{A/V}^2$.
 Find f_T if MOSFET is operating in triode region.

Sol)

$$\textcircled{1} C_{ox} = 3.45 \times 10^{-3} \text{ F/m}^2 = 3.45 \times 10^{-15} \text{ F}/\mu\text{m}^2$$

$$\textcircled{2} C_{gd} = C_{gs} = \frac{1}{2} WL C_{ox} + C_{ov} = \frac{1}{2} WL C_{ox} + WL_{ov} C_{ox} \\ = \left(\frac{1}{2} 10 \times 1 \times 3.45 \times 10^{-15} \right) + 10 \times 0.05 \times 3.45 \times 10^{-15} \\ = 17.25 \times 10^{-15} + 1.725 \times 10^{-15} = 18.975 \times 10^{-15} \text{ F} = 18.975 \text{ fF}$$

$$\textcircled{3} g_m = \sqrt{2k_n} \sqrt{W/L} \sqrt{I_D} = \sqrt{2 \times 150 \times 10^{-6}} \sqrt{10} \sqrt{1} \sqrt{200 \times 10^{-6}} = 0.7746 \text{ mA/V}$$

$$\textcircled{4} f_T = g_m / (2\pi(C_{gs} + C_{gd})) = 0.7746 \times 10^3 / (2\pi \times (18.975 + 18.975) \times 10^{-15}) = 3.24 \text{ GHz}$$